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Quadratic inequalities

A LEVEL LINKS

Scheme of work: 1d. Inequalities – linear and quadratic (including graphical solutions)

Key points

- First replace the inequality sign by = and solve the quadratic equation.
- Sketch the graph of the quadratic function.
- Use the graph to find the values which satisfy the quadratic inequality.

Examples

Example 1 Find the set of values of x which satisfy $x^2 + 5x + 6 > 0$



Example 2 Find the set of values of *x* which satisfy $x^2 - 5x \le 0$

$x^{2} - 5x = 0$ x(x - 5) = 0 x = 0 or x = 5	1 Solve the quadratic equation by factorising.
x = 0 or $x = 5$	2 Sketch the graph of $y = x(x-5)$
	3 Identify on the graph where $x^2 - 5x \le 0$, i.e. where $y \le 0$
$0 \le x \le 5$	4 Write down the values which satisfy the inequality $x^2 - 5x \le 0$

Example 3 Find the set of values of x which satisfy $-x^2 - 3x + 10 \ge 0$

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Practice

- 1 Find the set of values of x for which $(x + 7)(x 4) \le 0$
- 2 Find the set of values of x for which $x^2 4x 12 \ge 0$
- **3** Find the set of values of *x* for which $2x^2 7x + 3 < 0$
- 4 Find the set of values of x for which $4x^2 + 4x 3 > 0$
- 5 Find the set of values of x for which $12 + x x^2 \ge 0$

Extend

Find the set of values which satisfy the following inequalities.

- $\mathbf{6} \qquad x^2 + x \le \mathbf{6}$
- 7 x(2x-9) < -10
- **8** $6x^2 \ge 15 + x$

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Answers

- 1 $-7 \le x \le 4$
- $2 \qquad x \le -2 \text{ or } x \ge 6$
- **3** $\frac{1}{2} < x < 3$
- 4 $x < -\frac{3}{2} \text{ or } x > \frac{1}{2}$
- $5 \quad -3 \le x \le 4$
- $6 \quad -3 \le x \le 2$
- 7 $2 < x < 2\frac{1}{2}$ 8 $x \le -\frac{3}{2}$ or $x \ge \frac{5}{3}$